#### EXTENDS Naturals, Sequences, FiniteSets

#### Redeclaration of specdatamodels variables

VARIABLE events

CONSTANT USERS

CONSTANTS

Subscription Fee,

CancellationFee,

FailedPaymentFee

Logic to Test Replace stubs below with implementation. Because there is no forward declaration, we invert what we'd ideally like to do, which is to import the requirements into each implementation. Our logic testing relies on determining if a given state is enabled or not.

Variable database, month

INSTANCE stubs

 $Spec \stackrel{\Delta}{=} Init \wedge \Box [Next]_{vars}$ 

Trace requirements to specification

Not Traceable Functional: 1,2,3,6,7,9,14 NonFunctional: 1,2,3

#### Definitions

 $InTrial(u, end) \triangleq$ 

 $\exists i \in 1 \dots end$ :

 $\land events[i] \in StartTrialEvent$  Has started trial

 $\land events[i].user = u$ 

6. Start Trial endpoint request

6.3 If the requesting User has never been Subscribed or In Trial, that User SHALL be In Trial

 $\land \neg \exists j \in i ... end$ : And not canceled

 $\land events[j] \in$ 

8 Cancel Trial endpoint request

 $8.2~[{\rm Partial}]$  If the requesting User is In Trial, the User SHALL be Not Subscribed

 $CancelTrialEvent \cup$ 

2. Start Subscription endpoint request

2.2 If the requesting User is In Trial, the trial SHALL end and the requesting User SHALL be Subscribed

StartSubscriptionEvent

 $\land events[j].user = u$ 

```
\land events[j] \in MonthPassEvent
UnsubscribedAfterEvent(u, i, end) \stackrel{\Delta}{=}
    \exists j \in i \dots end: And not unsubscribed after
        \land events[j] \notin MonthPassEvent
        \land events[j].user = u
       Cancel Subscription endpoint request 4.2.1 User SHALL be Not Subscribed at the end of
           current month
        \land \lor \land events[j] \in CancelSubscriptionEvent
              \land \exists k \in j ... end : events[k] \in MonthPassEvent
          16. User has payment failed
          16.1 mark the User as Not Subscribed
           \lor events[j] \in PaymentFailedEvent
SubscribedFromStartSubscription(u, end) \triangleq
    2.4 If the requesting User is scheduled to be Not Subscribed due to cancellation, the requesting
        User SHALL remain Subscribed
    Implemented because a StartSubscriptionEvent after Cancel undoes the cancel
    \exists i \in 1 \dots end:
        \land events[i] \in StartSubscriptionEvent Has subscribed
        \land events[i].user = u
        \land \neg UnsubscribedAfterEvent(u, i, end)
AboutToCancel(u, end) \triangleq
    \exists i \in 1 \dots end:
        \land events[i] \in CancelSubscriptionEvent
        \land \neg \exists j \in i ... end:
            events[j] \in MonthPassEvent \cup
                           StartSubscriptionEvent
SubscribedFromTrial(u, end) \triangleq
    11 [Partial] When a User is In Trial at the end of the month that the trial was started, they
       SHALL be Subscribed
    \exists i \in 1 \dots end:
        \land events[i] \in StartTrialEvent Has started trial
        \land events[i].user = u
        \wedge \neg InTrial(u, end) Requirement fulfilled through InTrial
        \land \neg UnsubscribedAfterEvent(u, i, end)
```

11 [Partial] When a User is In Trial at the end of the month that the trial was started,

they SHALL be Subscribed

 $\land \neg \exists j \in i \dots end$ :

```
Cancel Trial endpoint request 8.2 [Partial] If the requesting User is In Trial, the User SHALL be Not Subscribed
```

$$\land \neg \exists j \in i \dots end : And not canceled  $\land events[j] \in CancelTrialEvent \land events[j].user = u$$$

$$Subscribed(u, end) \triangleq$$

 $\vee SubscribedFromStartSubscription(u, end)$ 

 $\vee SubscribedFromTrial(u, end)$ 

#### Invariants

#### 2 When a request is received by the Start Subscription endpoint

 $StartSubscriptionAccessControl \stackrel{\Delta}{=}$ 

 $\forall u \in \mathit{USERS}$ :

LET  $authorized \triangleq \neg Subscribed(u, Now) \lor AboutToCancel(u, Now)$ IN

2.1: If the requesting User is Subscribed, the request SHALL return with 409 Conflict

 $\lor \land \neg authorized$ 

 $\land \neg \text{ENABLED } StartSubscription(u)$ 

- 2.2 [Partial]: If the requesting User is In Trial, the trial SHALL end and the requesting User SHALL be Subscribed
- $2.3 \colon \text{If the requesting User is Not } \textit{Subscribed}, \text{ the requesting User SHALL be } \textit{Subscribed}$
- $\vee \wedge authorized$

 $\land$  ENABLED StartSubscription(u)

# 4 When a request is received by the Cancel Subscription endpoint

 $CancelSubscriptionAccessControl \stackrel{\Delta}{=}$ 

 $\forall u \in USERS$ :

LET  $authorized \triangleq Subscribed(u, Now) \land \neg AboutToCancel(u, Now)$ IN

 $4.1\ \mathrm{If}\ \mathrm{the}\ \mathrm{requesting}\ \mathrm{User}$  is not Subscribed, the request SHALL return with 409 Conflict

 $\lor \land \neg authorized$ 

 $\land \neg \text{ENABLED} \ Cancel Subscription(u)$ 

- 4.2 [Partial]: If the requesting User is Subscribed, the User SHALL ... [Cancellation Requirements]
- $\lor \land authorized$

 $\land$  ENABLED CancelSubscription(u)

#### 6.3 [Partial] If the requesting User is has never been Subscribed, or is In Trial

```
EligibleForTrial(u) \triangleq \\ \neg \exists \ i \in 1 \ .. \ Len(events) : \\ \land events[i] \in \\ StartSubscriptionEvent \cup \\ StartTrialEvent \\ \land events[i].user = u
```

### 6 When a request is received by the Start Trial endpoint

 $StartTrialAccessControl \triangleq$ 

 $\forall u \in USERS$ :

- 6.1 If the requesting User is Subscribed or In Trial, the request SHALL return with 409 Conflict
- $6.2~{\rm If}$  the requesting User has previously been Subscribed or In Trial, the request SHALL return with 409 Conflict
- $\lor \land \neg EligibleForTrial(u)$  $\land \neg ENABLED\ StartTrial(u)$
- $6.3~\mathrm{If}$  the requesting User has never been Subscribed or In Trial, that User SHALL be In Trial
- $\lor \land EligibleForTrial(u)$  $\land ENABLED\ StartTrial(u)$

#### 8 When a request is received by the Cancel Trial endpoint

 $CancelTrialAccessControl \triangleq$ 

 $\forall u \in \mathit{USERS}$ :

- 8.1 If the requesting User is not In Trial, the request SHALL return with 409 Conflict
- $\lor \land \neg InTrial(u, Now)$  $\land \neg ENABLED \ CancelTrial(u)$
- 8.2 [Partial] If the requesting User is In Trial, the User SHALL be Not Subscribed
- $\lor \land InTrial(u, Now)$  $\land ENABLED \ CancelTrial(u)$

# 10 When a request is received by the Watch Video endpoint

 $WatchVideoAccessControl \triangleq$ 

 $\forall u \in USERS$ :

- $10.1\ \mathrm{If}$  the requesting User is not In Trial or Subscribed, the request SHALL return with  $409\ \mathrm{Conflict}$
- $\lor \land \neg InTrial(u, Now) \land \neg Subscribed(u, Now) \land \neg Enabled Watch Video(u)$
- $10.2~\mathrm{If}$  the requesting User is In Trial or Subscribed, the system SHALL allow the User to Watch Video
- $\lor \land InTrial(u, Now) \lor Subscribed(u, Now)$  $\land ENABLED \ WatchVideo(u)$

```
Runs a given operation between: 1- first month for the first month, and month i- month i+1
TrueForEveryUserMonth(op(\_, \_, \_), checkFirstMonth) \stackrel{\Delta}{=}
    LET numMonthPass \stackrel{\Delta}{=} Cardinality(\{i \in 1 ... Len(events) : events[i]\}
                                                                    \in MonthPassEvent\}
    IN
      If checking the first month
     \land \lor \neg checkFirstMonth
        \lor \land checkFirstMonth
          There does not exist
            \land \neg \exists i \in 1 ... Len(events) :
               a first month
              \land events[i] \in MonthPassEvent
              \land \neg \exists j \in 1 \dots i : events[j] \in MonthPassEvent
               Where the op is false for any user
              \wedge \exists u \in USERS:
                  \neg op(u, 1, i)
      There does not exist a pair of consecutive months
     \wedge \neg \exists i \in 1 ... Len(events) :
          \land events[i] \in MonthPassEvent
          \land \exists j \in i+1 \dots Len(events):
              \land events[j] \in MonthPassEvent
              \wedge \neg \exists k \in (i+2) \dots (j-1):
                   events[k] \in MonthPassEvent
               where op is not true for all users
               \land \exists u \in \mathit{USERS} :
                  \neg op(u, i, j)
15 When a User is Billed the system SHALL call the Bill endpoint of the Payment Processor.
This requirement is satisfied by how requirements 4.2.2, 12 and 13 are tested. They test that
appropriate Bill message was dispatched
12 When a User becomes Subscribed
12.1 they shall be Billed the Subscription Fee before the end of the month
SubscribedThisMonth(u, start, end) \triangleq
     \wedge \neg Subscribed(u, start)
     \land Subscribed(u, end - 1)
UserSubscribedThisMonthBilledSubscriptionFee(u, start, end) \triangleq
    LET shouldBill \triangleq SubscribedThisMonth(u, start, end)IN
      Only applies if subscribed this month
     \vee \neg shouldBill
     \lor \land shouldBill
        \land \exists i \in start ... end :
```

```
\land events[i] \in BillEvent
             \land events[i].user = u
             \land \ events[i].fee = SubscriptionFee
SubscribedNewUsersBilledSubscriptionFee \stackrel{\Delta}{=}
    TrueForEveryUserMonth(UserSubscribedThisMonthBilledSubscriptionFee, TRUE)
13 When a User is Subscribed at the start of a month, they shall be Billed the Subscription Fee
SubscribedUserBilledThisMonth(u, start, end) \stackrel{\Delta}{=}
    LET subscribed \stackrel{\triangle}{=} Subscribed(u, start)IN
     Only applies if subscribed at start of month
     \vee \neg subscribed
     \lor \land subscribed
        \land \lor \exists i \in start ... end :
                \land events[i] \in BillEvent
                \land events[i].user = u
                \land events[i].fee = SubscriptionFee
           If the user failed a payment this is a separate workflow
           \vee \exists i \in start ... end:
                \land events[i] \in PaymentFailedEvent
                \land events[i].user = u
SubscribedUsersBilledStartOfMonth \stackrel{\triangle}{=}
    TrueForEveryUserMonth(SubscribedUserBilledThisMonth, FALSE)
       If the requesting User has Post Due Payments they SHALL be Billed in that amount before
       the end of the month, and Post Due Payments shall be zeroed
16 When a callback is received to the Payment Failed endpoint for a User, the system SHALL
   16.2 set Post Due Payment for the User to:
       (failed payment amount) + CancellationFee
PotentialStartingEvent(u, event) \stackrel{\Delta}{=}
     \land event \in StartSubscriptionEvent \cup
                  StartTrialEvent
     \land event.user = u
IsPaymentFailedEvent(u, event) \stackrel{\Delta}{=}
     \land event \in PaymentFailedEvent
     \land event.user = u
UserBilledForFailureBetweenRange(u, start, end, fee) \triangleq
    \exists i \in start ... end:
        \land events[i] \in BillEvent
        \land events[i].user = u
        \land events[i].fee = FailedPaymentFee
```

```
UserBilledForPostDuePaymentsIfSubscribed(u, start, end) \stackrel{\triangle}{=}
    LET starts \triangleq \{i \in 1 ... start : PotentialStartingEvent(u, events[i])\}IN
    LET paymentFailed \stackrel{\triangle}{=} \{i \in 1 ... start : IsPaymentFailedEvent(u, events[i])\}IN
    \forall p \in paymentFailed:
        Let resubscribedAfterFailedPayment \triangleq
             \exists i \in p \dots end :
                 \land i \in starts
        ΙN
        \vee \neg resubscribedAfterFailedPayment
        \lor \land resubscribedAfterFailedPayment
             There doesn't exist a failed payment
           \land \neg \exists i \in p \dots end :
                  That has a subscription directly after it
                 \land i \in starts
                 \land \neg \exists j \in p \dots i:
                      j \in starts
                  Where the user was not billed for the failed payment
                 \land \neg UserBilledForFailureBetweenRange(u, i, end, events[p].fee)
SubscribedUsersBilledPostDuePayements \stackrel{\Delta}{=}
     TrueForEveryUserMonth(UserBilledForPostDuePaymentsIfSubscribed, TRUE)
4 Cancel Subscription endpoint
4.2.2 if the user is Not Subscribed at the end of the current month, they SHALL be Billed a
Cancellation Fee
UserCancelledLastMonth(u, start, end) \stackrel{\Delta}{=}
      start-1 because it doesn't count cancellations that take effect
     \land Subscribed(u, start - 1)
     \land \neg Subscribed(u, start)
UserCancelledLastMonthBilled(u, start, end) \stackrel{\triangle}{=}
      Only applies if user cancelled this month
     \vee \neg UserCancelledLastMonth(u, start, end)
     \vee \wedge UserCancelledLastMonth(u, start, end)
        \land \lor \exists i \in start ... end :
                \land events[i] \in BillEvent
                \land events[i].user = u
                \land events[i].fee = CancellationFee
            If the user failed a payment this is a separate workflow
           \vee \exists i \in start ... end:
                \land events[i] \in PaymentFailedEvent
                \land events[i].user = u
```

 $CancelingUsersBilledCancelationFees \triangleq TrueForEveryUserMonth(UserCancelledLastMonthBilled, FALSE)$ 

# State Constraints

$$\begin{array}{ll} \textit{MonthLimit} \triangleq \\ & \text{LET} \ \textit{monthPassEvents} \triangleq \textit{SelectSeq}(\textit{events}, \text{LAMBDA} \ \textit{x} : \textit{x.type} = \text{"monthpass"}) \\ & \text{IN} \\ & \textit{Len}(\textit{monthPassEvents}) < 5 \end{array}$$

 $StateLimit \triangleq$ 

 $\land \textit{EventLengthLimit}$ 

 $\land \mathit{MonthLimit}$ 

 $<sup>\</sup>backslash * \ {\bf Modification} \ {\bf History}$ 

<sup>\\*</sup> Last modified Sun Jun 19 17:43:11 MST 2022 by elliotswart

 $<sup>\</sup>backslash \ ^*$  Created Thu Jun 16 19:34:18 MST 2022 by elliotswart