

Redeclaration of *specdatamodels* variables

EXTENDS *Sequences, Naturals, FiniteSets*

Represents every potential user in the system

CONSTANT *USERS*

Constants that should be set to single model values, to allow comparisons

Only equality comparisons will be made.

CONSTANTS

*SubscriptionFee,*  
*CancellationFee,*  
*FailedPaymentFee*

VARIABLES

Represents the current month

*month,*

Represents the status of the database. Design requirements require  
 that all persistent application state be stored here

*database,*

Required by spec

*events*

*vars*  $\triangleq$   $\langle$ *events, month, database* $\rangle$

Provides all the data models required by the spec

INSTANCE *specdatamodels*

*Now*  $\triangleq$  *Len(events)*

*Months*  $\triangleq$  0 .. 10

Strong Typing

*Month*  $\triangleq$  *Nat*

Database Rows

*UserRow*  $\triangleq$  [  
*subscribed* : BOOLEAN ,  
 Forget *cancelled*  
*inTrial* : BOOLEAN ,  
*trialStartTime* : *Nat*,  
*billedForMonth* : *Nat*,  
*hasHadTrialOrSubscription* : BOOLEAN ,  
*hasCancelled* : BOOLEAN ,

$$\begin{aligned}
& \text{cancelMonth} : \text{Nat} \\
& ] \\
\text{BillQueueItem} & \triangleq [ \\
& \text{user} : \text{USERS}, \\
& \text{fee} : \text{Fees} \\
& ] \\
\text{TypeOk} & \triangleq \\
& \wedge \text{EventsOk} \\
& \wedge \text{month} \in \text{Month} \\
& \wedge \text{database.users} \in [\text{USERS} \rightarrow \text{UserRow}] \\
& \wedge \text{database.billQueue} \in \text{Seq}(\text{BillQueueItem})
\end{aligned}$$

#### API endpoints

$$\begin{aligned}
\text{StartSubscription}(u) & \triangleq \\
& \text{Not subscribed} \\
& \wedge \wedge \text{database.users}[u].\text{subscribed} = \text{FALSE} \\
& \wedge \vee \text{database.users}[u].\text{inTrial} = \text{FALSE} \\
& \quad \vee \text{database.users}[u].\text{trialStartTime} = \text{month} \\
& \wedge \text{database}' = \\
& \quad [\text{database EXCEPT} \\
& \quad \quad !["users"][u].\text{subscribed} = \text{TRUE}, \\
& \quad \quad !["users"][u].\text{hasHadTrialOrSubscription} = \text{TRUE}, \\
& \quad \quad !["users"][u].\text{hasCancelled} = \text{FALSE} \\
& \quad ] \\
& \text{Observability required by stub} \\
& \wedge \text{events}' = \text{Append}(\text{events}, [\text{type} \mapsto \text{"startsubscription"}, \text{user} \mapsto u]) \\
& \wedge \text{UNCHANGED month}
\end{aligned}$$

$$\begin{aligned}
\text{CancelSubscription}(u) & \triangleq \\
& \text{Subscribed} \\
& \wedge \vee \text{database.users}[u].\text{subscribed} = \text{TRUE} \\
& \quad \vee \wedge \text{database.users}[u].\text{inTrial} = \text{TRUE} \\
& \quad \quad \wedge \text{database.users}[u].\text{trialStartTime} < \text{month} \\
& \wedge \text{database}' = \\
& \quad [\text{database EXCEPT} \\
& \quad \quad !["users"][u].\text{subscribed} = \text{FALSE}, \\
& \quad \quad !["users"][u].\text{inTrial} = \text{FALSE}, \\
& \quad \quad !["users"][u].\text{hasCancelled} = \text{TRUE}, \\
& \quad \quad !["users"][u].\text{cancelMonth} = \text{month}, \\
& \quad \quad \text{Charge cancellation fee} \\
& \quad ]
\end{aligned}$$

$$\begin{aligned} & ![\text{"billQueue"}] = \\ & \quad \text{Append}(\text{database.billQueue}, \\ & \quad \quad [user \mapsto u, fee \mapsto \text{CancellationFee}]) \\ & \end{aligned}$$

Observability required by stub  
 $\wedge \text{events}' = \text{Append}(\text{events}, [type \mapsto \text{"cancelsubscription"}, user \mapsto u])$   
 $\wedge \text{UNCHANGED } \langle month \rangle$

$$\begin{aligned} \text{StartTrial}(u) & \triangleq \\ & \wedge \text{database.users}[u].inTrial = \text{FALSE} \\ & \wedge \text{database.users}[u].subscribed = \text{FALSE} \\ & \wedge \text{database.users}[u].hasHadTrialOrSubscription = \text{FALSE} \\ & \wedge \text{database}' = [\text{database EXCEPT} \\ & \quad \quad ![\text{"users"}][u].inTrial = \text{TRUE}, \\ & \quad \quad ![\text{"users"}][u].trialStartTime = month, \\ & \quad \quad ![\text{"users"}][u].hasHadTrialOrSubscription = \text{TRUE} \\ & \quad \quad ] \end{aligned}$$

Observability required by stub  
 $\wedge \text{events}' = \text{Append}(\text{events}, [type \mapsto \text{"starttrial"}, user \mapsto u])$   
 $\wedge \text{UNCHANGED } \langle month \rangle$

$$\begin{aligned} \text{CancelTrial}(u) & \triangleq \\ & \text{In active trial} \\ & \wedge \text{database.users}[u].inTrial = \text{TRUE} \\ & \wedge \text{database.users}[u].trialStartTime = month \\ & \text{And not subscribed} \\ & \wedge \text{database.users}[u].subscribed = \text{FALSE} \\ & \wedge \text{database}' = [\text{database EXCEPT} \\ & \quad \quad ![\text{"users"}][u].inTrial = \text{FALSE} \\ & \quad \quad ] \end{aligned}$$

Observability required by stub  
 $\wedge \text{events}' = \text{Append}(\text{events}, [type \mapsto \text{"canceltrial"}, user \mapsto u])$   
 $\wedge \text{UNCHANGED } \langle month \rangle$

$$\begin{aligned} \text{WatchVideo}(u) & \triangleq \\ & \wedge \vee \text{database.users}[u].subscribed = \text{TRUE} \\ & \quad \vee \text{database.users}[u].inTrial = \text{TRUE} \\ & \quad \text{Remove video access at the end of cancelled month} \\ & \quad \vee \wedge \text{database.users}[u].hasCancelled = \text{TRUE} \\ & \quad \quad \wedge \text{database.users}[u].cancelMonth = month \end{aligned}$$

Observability required by stub

$\wedge events' = Append(events, [type \mapsto \text{"watchvideo"}, user \mapsto u])$   
 $\wedge UNCHANGED \langle month, database \rangle$

Stub method, do not changed

$Bill(u, fee) \triangleq$   
 $\wedge events' = Append(events, [type \mapsto \text{"bill"},$   
 $user \mapsto u,$   
 $fee \mapsto fee])$

$PaymentFailed(u, fee) \triangleq$   
 $\wedge database' = [database \text{ EXCEPT}$   
 $!["users"][u].subscribed = FALSE,$   
 $!["users"][u].hasCancelled = FALSE$   
 $]$

Observability required by stub

$\wedge events' = Append(events, [type \mapsto \text{"paymentfailed"},$   
 $user \mapsto u,$   
 $fee \mapsto fee])$   
 $\wedge UNCHANGED \langle month \rangle$

#### Recurring Operations

This the the state that calls the Payment Failed API

$ExistingBillFailed \triangleq$   
 $\vee \exists i \in 1 .. Len(events) :$   
 $\quad \text{Only a past bill can fail}$   
 $\quad \wedge events[i] \in BillEvent$   
 $\quad \wedge PaymentFailed(events[i].user, events[i].fee)$

$BillSubscribedUsers \triangleq$   
 $\wedge \exists u \in USERS :$   
 $\quad \text{That is subscribed}$   
 $\quad \wedge \vee database.users[u].subscribed = TRUE$   
 $\quad \quad \text{Subscribed from a trial so bill}$   
 $\quad \vee \wedge database.users[u].inTrial = TRUE$   
 $\quad \quad \wedge database.users[u].trialStartTime < month$   
 $\quad \text{Ensure users are not double billed}$   
 $\quad \wedge database.users[u].billedForMonth < month$   
 $\quad \wedge database' =$   
 $\quad [database \text{ EXCEPT}$   
 $\quad \quad \text{Add subscription fee}$   
 $\quad \quad !["billQueue"] =$   
 $\quad \quad \quad Append(database.billQueue,$   
 $\quad \quad \quad [user \mapsto u, fee \mapsto SubscriptionFee]),$   
 $\quad \quad !["users"][u].billedForMonth = month$

$$\begin{aligned}
& ] \\
& \wedge \text{UNCHANGED } \langle \text{events}, \text{month} \rangle \\
\text{ProcessBills} & \triangleq \\
& \wedge \text{Len}(\text{database.billQueue}) > 0 \\
& \wedge \text{LET } \text{bill} \triangleq \text{Head}(\text{database.billQueue}) \text{ IN} \\
& \quad \text{Bills user} \\
& \quad \wedge \text{Bill}(\text{bill.user}, \text{bill.fee}) \\
& \quad \wedge \text{database}' = \\
& \quad \quad [ \text{database EXCEPT} \\
& \quad \quad \quad \text{Removes head of queue} \\
& \quad \quad \quad ![\text{"billQueue"}] = \\
& \quad \quad \quad \quad \text{SubSeq}(\text{database.billQueue}, \\
& \quad \quad \quad \quad \quad 2, \text{Len}(\text{database.billQueue})) \\
& \quad \quad ] \\
& \wedge \text{UNCHANGED } \langle \text{month} \rangle
\end{aligned}$$

Stub method that prevents the month from passing until all operations are complete. Represent worker methods, etc

$$\begin{aligned}
\text{HandledMonth} & \triangleq \\
& \wedge \neg \text{ENABLED } \text{BillSubscribedUsers} \\
& \wedge \neg \text{ENABLED } \text{ProcessBills}
\end{aligned}$$

DO NOT MODIFY

$$\begin{aligned}
\text{MonthPasses} & \triangleq \\
& \wedge \text{HandledMonth} \\
& \wedge \text{month}' = \text{month} + 1 \\
& \wedge \text{events}' = \text{Append}(\text{events}, [\text{type} \mapsto \text{"monthpass"}]) \\
& \wedge \text{UNCHANGED } \langle \text{database} \rangle
\end{aligned}$$

Specification

$$\begin{aligned}
\text{Init} & \triangleq \\
& \wedge \text{events} = \langle \rangle \quad \text{Events must be intialized empty, per stub} \\
& \wedge \text{month} = 0 \\
& \wedge \text{database} = [ \\
& \quad \text{Users start with everything unset} \\
& \quad \text{users} \mapsto \\
& \quad \quad [ \text{u} \in \text{USERS} \mapsto \\
& \quad \quad \quad [ \\
& \quad \quad \quad \quad \text{subscribed} \mapsto \text{FALSE}, \\
& \quad \quad \quad \quad \text{inTrial} \mapsto \text{FALSE}, \\
& \quad \quad \quad \quad \text{trialStartTime} \mapsto 0, \\
& \quad \quad \quad \quad \text{billedForMonth} \mapsto 0, \\
& \quad \quad \quad \quad \text{hasHadTrialOrSubscription} \mapsto \text{FALSE}, \\
& \quad \quad \quad \quad \text{hasCancelled} \mapsto \text{FALSE}, \\
& \quad \quad \quad \quad \text{cancelMonth} \mapsto 0 \\
& \quad \quad \quad ] \\
& \quad \quad ] \\
& \quad ]
\end{aligned}$$

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    ]
  ],
  Bill queue starts empty
  billQueue  $\mapsto$   $\langle \rangle$ 
]

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Next  $\triangleq$ 
  \* Required by stub
  \ MonthPasses
  \* State modified below
  \  $\exists u \in USERS$ :
    \ StartSubscription(u)
    \ CancelSubscription(u)
    \ StartTrial(u)
    \ CancelTrial(u)
    \ WatchVideo(u)
  \* Add more user based states
  \* Payment failing behavior is part of spec not implementation
  \ ExistingBillFailed
  \ BillSubscribedUsers

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\* Modification History
\* Last modified Sun Jun 19 17:44:01 MST 2022 by elliotswart
\* Created Sun Jun 19 16:56:29 MST 2022 by elliotswart

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